An action/state-based model-checking approach for the analysis of an asynchronous protocol for Service-Oriented Applications

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Abstract. In this paper we present an action/state-based logical framework for the analysis and verification of complex systems, which relies on the definition of doubly labelled transition systems. The defined temporal logic, called UCTL, combines the action paradigm—classically used to describe systems using labelled transition systems—with predicates that are true over states—as captured when using Kripke structures as semantic model. An efficient model checker for UCTL has been realized, exploiting an on-the-fly algorithm. We then show how to use UCTL and its model checker in the design phase of an asynchronous extension of SOAP, called aSOAP. For this purpose, we describe aSOAP as a set of communicating UML state machines, for which a semantics over doubly labelled transition systems has been provided.

1 Introduction

Complex systems are often modelled according to either a state-based or an event-based paradigm. While in the former case the system is characterized by states and state changes, in the latter case it is characterized by the events (actions) that can be performed to move from one state to another. Both are important paradigms for the specification of complex systems and, as a result, formal methods ideally should cover both. Indeed, this trend is witnessed by the recent widespread use of modelling frameworks that allow both events and state changes to be specified. An example are UML state diagrams, which are used more and more in industry to specify the behaviour of (software) systems, though often without caring much for their formal aspects. Also the specification of Service-Oriented Applications has seen several applications of UML state diagrams [21]. What is missing in order to use in full specification techniques that allow one to specify both events and state changes, is the availability of a formal framework in which desired properties can subsequently be proved over the specification, with the support of specific verification tools.

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In this paper, we aim to fill this gap by presenting the action/state-based temporal logic UCTL, which allows one to both specify the basic properties that a state should satisfy and to combine these basic predicates with advanced temporal operators dealing with the events performed. The semantic domain of UCTL is doubly labelled transition systems [9]. A prototypical on-the-fly model checker, UMC [11], has been developed for this logic: the tool allows the efficient verification of UCTL formulae that define action/state-based properties.

In recent years, several other logics that allow one to express both action-based and state-based properties have been introduced, for different purposes than ours. An event- and state-based temporal logic for Petri nets is introduced in [14]. In [13], a modal temporal logic without a fixed-point operator and interpreted over so-called Kripke modal transition systems, a modal version of doubly labelled transition systems, is defined. In [2, 3], a state/event extension of LTL is presented, together with a model checking framework, whose formulae are interpreted over so-called labelled Kripke structures, which are in essence doubly labelled transition systems. Finally, in [4], this linear-time temporal logic is extended to a universal branching-time temporal logic. The latter logics are being used extensively to verify software system.

The advantage of all such logics lies in the ease of expressiveness of properties that in pure action-based or pure state-based logics can be quite cumbersome to write down. Furthermore, more often than not, their use results in a reduction of the state space, the memory use and the time spent for verification. Obviously, the real gain depends—as always—on the specific system under scrutiny.

To conclude, a case study shows the use of UCTL and its model checker UMC in the design phase of an asynchronous extension of the web service communication protocol SOAP, which we call aSOAP. Mobile communication networks typically are unstable, since terminal devices can dynamically change reachability status during their lifetime. In Service-Oriented Architectures, asynchronous service invocation is often the more suitable paradigm for the choreography and orchestration of their mobile components. Hence there is a need for communication protocols that can manage asynchronous communication also in the presence of unstable network connections. Formal modelling and analysis of these protocols is a first step towards the successful implementation and evaluation of reliable Service-Oriented Applications. For this purpose, we describe aSOAP as a set of communicating UML state machines, for which a semantics over doubly labelled transition systems has been provided, express several behavioural properties on this UML model of aSOAP in UCTL and verify them with UMC.

The paper is organized as follows. Some preliminary definitions are given in Section 2. In Section 3 we present the syntax and semantics of UCTL and we briefly describe its model checker UMC. The case study illustrating the use of UMC is presented in Section 4. Finally, Section 5 concludes the paper.

2 Preliminaries

In this section, we define the basic notations and terminology used in the sequel.
Definition 1 (Labelled Transition System). A Labelled Transition System (LTS for short) is a quadruple \((Q, q_0, \text{Act}, R)\), in which:

- \(Q\) is a set of states;
- \(q_0 \in Q\) is the initial state;
- \(\text{Act}\) is a finite set of observable events (actions) with \(e\) ranging over \(\text{Act}\), \(\alpha\) ranging over \(2^{\text{Act}}\) and \(\epsilon\) denoting the empty set;
- \(R \subseteq Q \times 2^{\text{Act}} \times Q\) is the transition relation; instead of \((q, \alpha, q') \in R\) we often write \(q \xrightarrow{\alpha} q'\).

Note that the main difference between this definition of LTSs and the classical one is the labelling of the transitions: we label transitions by sets of events rather than by single (un)observable events. This extension allows the transitions from one state to another to represent sets of actions without the need of intermediate states, which has proved to be useful when modelling, e.g., UML state diagrams.

Another extension is the labelling of states with atomic propositions, following the concept of doubly labelled transition systems [9], again extended as in Definition 1.

Definition 2 (Doubly Labelled Transition System). A Doubly Labelled Transition System (L\(^2\)TS for short) is a quintuple \((Q, q_0, \text{Act}, R, \mathcal{L})\), in which:

- \((Q, q_0, \text{Act}, R)\) is an LTS;
- \(\mathcal{L} : Q \rightarrow 2^{\mathcal{AP}}\) is a labelling function that associates a subset of the set of atomic propositions \(\mathcal{AP}\) to each state of the LTS.

An atomic proposition \(p \in \mathcal{AP}\) will typically have the form of an expression like \(\text{VAR} = \text{value}\).

The L\(^2\)TSs thus obtained are very similar to so-called Kripke transition systems [16]. The latter are defined as an extension of Kripke structures by a labelling over transitions.

The usual notion of bisimulation equivalence can be straightforwardly extended to L\(^2\)TSs by taking into account equality of labelling of states, and considering the transitions labelled by sets of events.

Definition 3 (Bisimulation). Let \(\mathcal{A}_1 = (Q_1, q_{01}, \text{Act}, \xrightarrow{1}, \mathcal{L}_1)\) and \(\mathcal{A}_2 = (Q_2, q_{02}, \text{Act}, \xrightarrow{2}, \mathcal{L}_2)\) be two L\(^2\)TSs and let \(q_1 \in Q_1\) and \(q_2 \in Q_2\). We say that the two states \(q_1\) and \(q_2\) are strongly equivalent (or simply equivalent), denoted by \(q_1 \sim q_2\), if there exists a strong bisimulation \(\mathcal{B}\) that relates \(q_1\) and \(q_2\).

\(\mathcal{B} \subseteq S_1 \times S_2\) is a strong bisimulation if for all \((q_1, q_2) \in \mathcal{B}\) and \(\alpha \in 2^{\text{Act}}:\)

1. \(\mathcal{L}_1(q_1) = \mathcal{L}_2(q_2)\),
2. \(q_1 \xrightarrow{\alpha} q_1'\) implies \(\exists q_2' \in Q_2 : q_2 \xrightarrow{\alpha} q_2'\) and \((q_1', q_2') \in \mathcal{B}\), and
3. \(q_2 \xrightarrow{\alpha} q_2'\) implies \(\exists q_1' \in Q_1 : q_1 \xrightarrow{\alpha} q_1'\) and \((q_1', q_2') \in \mathcal{B}\).

We say that the two L\(^2\)TSs \(\mathcal{A}_1\) and \(\mathcal{A}_2\) are equivalent, denoted by \(\mathcal{A}_1 \sim \mathcal{A}_2\), if there exists a strong bisimulation \(\mathcal{B}\) such that \((s_{01}, s_{02}) \in \mathcal{B}\).
The usual notions of simulation preorder or weak (observational) equivalence can be defined analogously. LTSs and Kripke structures can be lifted to $L^2$TSs in a straightforward manner. An LTS $T = (Q, q_0, Act, \rightarrow)$ can be lifted to an $L^2$TS $A_T$, on the same set of states and maintaining the same transition relation, in the following way: $A_T = (Q, q_0, Act, \rightarrow, L)$, where for all $s \in Q$: $L(s) = AP$.

A Kripke structure $K = (Q, q_0, \rightarrow, L)$ can be lifted to an $L^2$TS $A_K$, on the same set of states and maintaining the same labelling function, in the following way: $A_K = (Q, q_0, Act, \rightarrow', L)$, where $s \rightarrow s'$ implies $s \overset{\pi}{\rightarrow}' s'$.

### 3 The Action/State-Based Temporal Logic UCTL

In this section we present the syntax and semantics of UCTL. This temporal logic, action and state based, allows one to reason on state properties as well as to describe the behaviour of systems that perform actions during their lifetime. UCTL includes both the branching-time action-based logic ACTL [8, 9] and the branching-time state-based logic CTL [5].

Before defining the syntax of UCTL, we introduce an auxiliary logic of events.

**Definition 4 (Event formulae).** Let Act be a set of observable events. Then the language of event formulae on Act $\cup \\{\tau\}$ is defined as follows:

$$\chi ::= tt | e | \tau | \neg \chi | \chi \land \chi$$

**Definition 5 (Event formulae semantics).** The satisfaction relation $|= \alpha \models \chi$ for event formulae of the form $\alpha \models \chi$ is defined over sets of events as follows:

- $\alpha \models tt$ holds always;
- $\alpha \models e$ iff $\alpha = \{e_1, \ldots, e_n\}$ and there exists an $i \in \{1, \ldots, n\}$ such that $e_i = e$;
- $\alpha \models \tau$ iff $\alpha = \emptyset$;
- $\alpha \models \neg \chi$ iff not $\alpha \models \chi$;
- $\alpha \models \chi \land \chi'$ iff $\alpha \models \chi$ and $\alpha \models \chi'$.

As usual, $\neg tt$ abbreviates $\neg tt$ and $\chi \lor \chi'$ abbreviates $\neg (\neg \chi \land \neg \chi')$.

**Definition 6 (Syntax of UCTL).**

$$\phi ::= true | p | \phi \land \phi' | \neg \phi | A \pi | E \pi$$

$$\pi ::= X \chi \phi | \phi \land \phi' | \phi \land U \chi \phi'$$

State formulae are ranged over by $\phi$, path formulae are ranged over by $\pi$, $A$ and $E$ are path quantifiers, and $X$ and $U$ are indexed next and until operators.\(^3\)

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\(^3\) Note that ACTL is also used to denote the universal fragment of CTL, originally called ∀CTL in [6]. For easy of writing, ∀CTL was changed to ACTL, thus generating a conflict with the previously introduced acronym ACTL for Action-based CTL.

\(^4\) Note that, differently from the original ACTL logic, in UCTL the operator $X \chi \phi$ can be derived as $false \land \land U \chi \phi$. 

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4
To define the semantics of UCTL, we need the notion of a path in an L$^2$TS.

**Definition 7 (Path).** Let $A = (Q, q_0, Act, R, L)$ be an L$^2$TS and let $s \in Q$.

- $\sigma$ is a path from $s$ if $s = s$ (the empty path from $s$) or $\sigma$ is a (possibly infinite) sequence $(s_0, \alpha_1, s_1)(s_1, \alpha_2, s_2) \cdots$ with $(s_{i-1}, \alpha_i, s_i) \in R$ for all $i > 0$.
- The concatenation of paths $\sigma_1$ and $\sigma_2$, denoted by $\sigma_1 \sigma_2$, is a partial operation, defined only if $\sigma_1$ is finite and its final state coincides with the first state of $\sigma_2$. Concatenation is associative and has identities: $\sigma_1(\sigma_2 \sigma_3) = (\sigma_1 \sigma_2) \sigma_3$ and if $s_0$ is the first state of $\sigma$ and $s_n$ is its final state, then $s_0 \sigma = \sigma s_n = \sigma$.
- A path $\sigma$ is said to be maximal if it is either an infinite sequence or it is a finite sequence whose final state has no successor states.
- The length of a path $\sigma$ is denoted by $|\sigma|$. If $\sigma$ is an infinite path, then $|\sigma| = \omega$. If $\sigma = s$, then $|\sigma| = 0$. If $\sigma = (s_0, \alpha_1, s_1)(s_1, \alpha_2, s_2) \cdots (s_n, \alpha_{n+1}, s_{n+1})$, for some $n \geq 0$, then $|\sigma| = n + 1$. Moreover, the $i$th state in such a path, i.e. $s_i$, is denoted by $\sigma(i)$.

**Definition 8 (Semantics of UCTL).** The satisfaction relation for UCTL formulae is defined as follows:

1. $q \models true$ holds always;
2. $q \models p$ iff $p \in L(q)$;
3. $q \models \neg \phi$ iff $q \not\models \phi$;
4. $q \models \phi \land \phi'$ iff $q \models \phi$ and $q \models \phi'$;
5. $\sigma \models X\chi \phi$ iff $\sigma = (\sigma(0), \alpha_1, \sigma(1))\alpha'$, and $\alpha_1 \models \chi$, and $\sigma(1) \models \phi$;
6. $\sigma \models [\phi]U\alpha' \phi'$ iff there exists a $j \geq 0$ such that $\sigma(j) \models \phi'$ and for all $0 \leq i < j$: $\sigma = \sigma'(\sigma(i), \alpha_{i+1}, \sigma(i+1))\sigma''$ implies $\sigma(i) \models \phi$ and $\alpha_{i+1} = \epsilon$ or $\alpha_{i+1} \models \chi$;
7. $\sigma \models [\phi]U\alpha' \phi'$ iff there exists a $j \geq 1$ such that $\sigma = \sigma'(\sigma(j-1), \alpha_j, \sigma(j))\alpha''$ and $\sigma(j-1) \models \phi$ and $\alpha_j \models \chi$, and for all $0 < i < j$: $\sigma = \sigma'(\sigma(i-1), \alpha_i, \alpha(i))\alpha''$ implies $\sigma(i-1) \models \phi$, and $\alpha_i = \epsilon$ or $\alpha_i \models \chi$.

It is straightforward to obtain a set of derived operators for UCTL, such as:

- $< \chi > \phi$ stands for $E[true \ U\chi \phi]$;
- $[\chi]\phi$ stands for $\neg < \chi > \neg \phi$;
- $EF\phi$ stands for $E[true \ U\phi]$;
- $AG\phi$ stands for $\neg EF\neg \phi$.

Operators $< \chi > \phi$ and $[\chi]\phi$ are the diamond and box modalities of the Hennessy-Milner logic [12]. The meaning of $EF\phi$ is that $\phi$ must be true sometimes in a possible future; that of $AG\phi$ is that $\phi$ must be true always.

The logic UCTL is adequate with respect to strong bisimulation equivalence on L$^2$TSs. The proof of adequacy is an extension of the one given in [8] for ACTL, considering L$^2$TSs rather than LTSs. Adequacy [18] means that two L$^2$TSs $A_1$ and $A_2$ are strongly bisimilar if and only if $F_1 = F_2$, where $F_i = \{ \psi \in UCTL : A_i \models \psi \}$ for $i = 1, 2$.

Starting from the syntax of UCTL, it is possible to derive both CTL [5] and ACTL [8, 9] by simply removing the action or the state component, respectively.
Given a Kripke structure \( K = (Q, q_0, \rightarrow, \mathcal{L}) \) that has been lifted to an \( L^2TS \) \( \mathcal{A}_K = (Q, q_0, \text{Act}, \rightarrow', \mathcal{L}) \), a CTL formula \( \phi \) and a state \( s \in Q \), it follows that

\[
s \models_K \phi \iff s \models_{\mathcal{A}_K} \phi',
\]

where \( \phi' \) is a UCTL formula which is syntactically identical to \( \phi \), apart from the fact that all occurrences of \( X\psi' \) have been replaced by \( X_{true}\psi' \) and all occurrences of \( \psi U \psi' \) have been replaced by \( \psi_{true} U \psi' \).

Given an LTS \( T = (Q, q_0, \text{Act} \cup \tau, \rightarrow) \) that has been lifted to an \( L^2TS \) \( \mathcal{A}_T = (Q, q_0, \text{Act}, \rightarrow, \mathcal{L}) \), an ACTL formula \( \phi \) and a state \( s \in Q \), it follows that

\[
s \models_T \phi \iff s \models_{\mathcal{A}_T} \phi',
\]

where \( \phi' \) is a UCTL formula which is syntactically identical to \( \phi \), apart from the fact that all occurrences of \( X_{true}\psi \) are replaced by \( X_{\neg \tau}\psi \).

### 3.1 UCTL Model Checking

We have developed an on-the-fly model checking tool for UCTL, called UMC [15]. The basic idea behind UMC is that, given a state of an \( L^2TS \), the validity of a UCTL formula on that state can be evaluated by analyzing the transitions allowed in that state, and by analyzing the validity of some subformula in only some of the next reachable states, all this in a recursive way. As a result, depending on the formula, only a fragment of the overall state space might need to be generated and analyzed to be able to produce the correct result. This type of model checking is also called local [7], in contrast to global model checking [5], in which the whole state space is explored to check the validity of a formula. The complexity results of UMC are those expected according to [10]. Indeed, we have linear-time complexity for the evaluation of UCTL formulae.

The development of UMC is still in progress and a prototypical version is being used internally at ISTI–CNR for academic and experimental purposes. So far, the focus of the development has been on the design of the kind of qualitative features one would desire for such a tool, experimenting with various logics, system modelling languages and user interfaces. The quantitative aspects of such a tool, e.g. concerning optimizations aimed at limiting state-space explosions or the complexity of the evaluation algorithms (to their known minimal limits), have not yet been taken into consideration. Nor has there been an official public release of the tool, even if the current prototype can be experimented via a web interface at the address http://fmt.isti.cnr.it/umc/.

UMC verifies properties defined over a set of communicating UML state machines [19, 17]. We used UML as particular formal method since it has become the de facto industrial standard for modelling and documenting software systems. The UML semantics associates a state machine to each object in a system.

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5 The original definition of ACTL [8] is based on a definition of LTSs in which a transition label can be a single (un)observable action. Hence, to be precise, we actually need to use here a different definition of lifting an LTS to an \( L^2TS \), namely one in which \( \tau \)-transitions are replaced by \( \epsilon \)-transitions.
design, while the system’s behaviour is defined by the possible evolutions of the resulting set of state machines that may communicate by exchanging signals. All these possible system evolutions are formally represented as an $L^2$TS, in which the states represent the various system configurations and the transitions represent the possible evolutions of a system configuration. In this $L^2$TS, states are labelled with the observed structural properties of the system configurations (e.g. active substates of objects, values of object attributes, etc.), while transitions are labelled with the observed properties of the system evolutions (e.g. which is the evolving object, which are the executed actions, etc.).

4 aSOAP: A Case Study

The particular case study we describe here has as main objective to define a variant of SOAP [22] supporting asynchronous communications, driven step-by-step by the results of a formal analysis. This approach thus contrasts with the usual approach of performing analysis on an already specified protocol to verify its correctness. The development of aSOAP is ongoing joint work with Telecom Italia. Some initial modelling and verification results have been presented in [1].

The domain of the case study is the definition of a SOAP-based protocol supporting asynchronous interactions, i.e. interactions different from the usual synchronous “request-response” interactions supported by the available SOAP implementations based on HTTP. For the following reasons, asynchronous interactions are highly relevant in the delivery of telecommunication services:

- a service logic is triggered/activated by events produced, in an asynchronous way, by the network/special resources, or must react to such events during the execution of a service instance;
- requests produced by a service logic to a network/special resource may result in long computations (e.g. the set-up of a call), which might also require the involvement of end users;
- some service logic components may not be reachable (e.g. the ones deployed on mobile terminals), e.g. due to the temporary absence of communication.

The final objective is thus to formally define aSOAP as a protocol that is able to address most of these situations. We consider the following requirements.

**Backward compatibility:**
- aSOAP must be compatible with SOAP v1.2 on HTTP;
- aSOAP must have limited impact on clients, i.e. clients that need no support for asynchronous interactions must be usual SOAP clients, working in request-response mode, while clients that do need such support should introduce only very limited variations w.r.t. normal SOAP requests.

**Reachability:**
- aSOAP must be able to deal with the unreachability of the servers (e.g. due to the lack of connectivity);
- aSOAP must be able to deal with the case in which a server cannot return a (provisional or final) response due to the lack of connectivity;
aSOAP must be able to deal with the case in which a (provisional or final) response cannot be returned to a client due to the lack of connectivity.

**Message Exchange Patterns**:
- aSOAP must be able to deal with requests that require the servers to perform some long-running computation (longer than the HTTP timeout) before producing any results;
- aSOAP must be able to deal with requests with multiple responses.

We envision aSOAP to operate in a Client-Server architecture with an additional web service Proxy placed in between the Client and Server side. This Proxy must guarantee that various attempts to contact either side are made in case of temporary unavailability of the respective side. Moreover, aSOAP requires that a Client, whenever it is willing to accept the possibility of an asynchronous response to its request, sends to the Proxy not only its request but also the URL at which it would like to receive the response. We consider this URL to be the address of a generic “SOAP listener” and we assume the application level to be equipped with a mechanism capable of receiving SOAP messages at this URL.

Before discussing some aspects of our formal specification of aSOAP, we first list the assumptions that are part of the design of aSOAP.

- The Proxy is always reachable by both the Client and the Server, whenever they have an active connection;
- If the Client is willing to accept an asynchronous response to its SOAP invocation, then it inserts in the SOAP header the URL of the SOAP listener where it wants to receive the response;
- The URL in the header of an asynchronous SOAP invocation is the address of a generic SOAP listener and the application level is equipped with a mechanism for receiving SOAP messages at this URL;
- Upon receiving an asynchronous SOAP invocation from the Client, the Proxy generates a request identifier ReqId that uniquely identifies the Client’s SOAP invocation in further communications.

During several sessions between ISTI–CNR and Telecom Italia we discussed our design and developed our formalisation of aSOAP in detail. In order to facilitate the discussions about the behaviour of the various use case scenarios of aSOAP, we decided upon a separate message sequence chart for each such a scenario. Finally, all these scenarios were translated into an operational model, in which the following concrete modelling choices were adopted:

- All SOAP invocations are asynchronous, i.e. we abstract from the synchronous SOAP invocations that only serve to guarantee backward compatibility with SOAP v1.2;
- The URL in the header of a SOAP message is identified with the Client, i.e. each Client is seen as just a listener of asynchronous SOAP invocations;
- A system model is constituted by a Server (and its subthreads), a Proxy (and its subthreads) and a fixed (configurable) number of Clients;
- The Proxy and the Server may activate at most a fixed (configurable) number of parallel subthreads;
With the Client or the Server unreachable, the Proxy attempts to contact them up to a configurable number of times;

- The Client issues a single SOAP invocation and then terminates.\footnote{In the future we do intend to consider Clients that perform a loop of SOAP invocations or issue several SOAP invocations before awaiting the deferred SOAP results.}

For a complete discussion on these modelling choices, we refer the reader to [1].

To use UMC, we specified the formal model of aSOAP as a set of communicating UML state machines. This allows us to express behavioural properties of our aSOAP model in UCTL and to verify them with UMC, which we do in the next section. The reader can consult the full specification online [20]. In Figure 1, the activity of a Client, a Server thread and a Proxy thread are depicted.

The full specification contains also the definition of the statecharts for the classes Server and Proxy. Objects of these classes are very simple (they have just one state) and their role is simply to forward any incoming request to some available subthread, which will then perform all the relevant activities. The actual complexity of the systems which can be built with these components clearly depends on the number of Clients, Servers and Proxies that one wants to deploy, on the number of subthreads one assigns to each Server or Proxy and on the maximum number of times a Proxy thread may retry to contact a Server or a Client before it must give up.

The minimal system composed of 1 Client, 1 Proxy and 1 Server (the latter two both with only 1 subthread) and 1 as maximum number of retries, clearly is an example of a small system with only 118 states and 245 transitions. A more complex system can be deployed by using 2 Clients, 1 Server and 1 Proxy (the latter two with 2 subthreads each), and with up to 2 communication attempts. Such a system contains 96,481 states and 367,172 transitions. Finally, a system composed of 3 Clients, 1 Server and 1 Proxy (the latter two with 3 subthreads each) instead is too complex to be able to explicitly measure its size (far more than 600,000 states and well over 1,000,000 transitions).

### 4.1 Verification of UCTL Formulae with UMC

In this section, we show the verification with UMC of several behavioural properties expressed in UCTL over our model of the aSOAP protocol. These properties demonstrate the logic’s flexibility in dealing with both action- and state-based properties. A different set of behavioural properties is verified in [1]. Property 1:

*From every system state a Proxy thread can reach its initial state ‘Ready’*

can be shown to hold by using UMC to verify the state-based UCTL formula

$$\text{AG EF } PT1.\text{state} = \text{Ready},$$

in which $PT1$ is a Proxy Thread. This is different for Clients, since Property 2:

*A Client C1 may reach a deadlock, i.e.*

there exists a system state from which $C1$ cannot evolve
Fig. 1. Activity of a Client, a Server thread and a Proxy thread.
can be shown to hold by using UMC to verify the action-based UCTL formula

\[ EF (\neg EF < C1: > true), \]

in which \( C1 \) is satisfied by any system evolution in which object \( C1 \) is the one that evolves. This outcome is not so bad as it might seem, because Property 3:

**Whenever a Client \( C1 \) reaches a deadlock,**

then \( C1 \) is either in state ‘Wait’ or in state ‘Deferred’

can be shown to hold by using UMC to verify the action/state-based UCTL formula

\[ AG ( (\neg EF < C1: > true) \Rightarrow (C1.state = Wait \lor C1.state = Deferred) ). \]

The time needed to verify any of the above formulae in the minimal system mentioned above (with 118 states and 245 transitions) is negligible. The situation is different for the system with 2 Clients specified above (with 96, 481 states and 367, 172 transitions). In spite of its higher complexity, the evaluation of the formula \( EF (\neg EF < C1: > true) \) (corresponding to Property 2) is still almost immediate, since it requires the analysis of only 1998 states, while the remaining formulae require the analysis of all system states and therefore their evaluation requires about one minute (using a modern portable computer).

Finally, none of the above formulae can be verified over more complex systems. However, formulae whose evaluation require the analysis of just a small fraction of all the system states can be evaluated also for such complex systems. Consider, e.g., the formula

\[ EF EG ((PT1.state = ClientLoop2) \land < PT1: > (PT1.state = Ready)), \]

which states that there exists an infinite path along which object \( PT1 \) always remains in the \( ClientLoop2 \) state, although the object itself always has the possibility of immediately returning to the state \( Ready \) in just one step. This formula can be proved to hold also in case of a complex system composed of 3 Clients, 1 Server and 1 Proxy (but each with 3 subthreads), which has more than 600,000 states and over 1,000,000 transitions. It takes just a few seconds, during which only 92,536 system states are analysed. Clearly it is simply a form of unfairness in the scheduling that prevents the Proxy thread to complete its execution cycle.

5 **Conclusions**

In this paper, we have presented the action/state-based temporal logic UCTL. The need to define an action/state-based logic stems from the fact that in order to verify concurrent (software) systems, it is quite often necessary to specify both state information and the evolution in time by actions (events). As a result, semantic models should take both views into account. The \( L^2TSs \) that are at the basis of UCTL are one such semantic model.
UML is a graphical modelling language for object-oriented software (systems). UML models can be used to visualize, specify, build and document several aspects—or views—of such systems. The UML semantics associates to each active object a state machine, and the system’s behaviour is defined by the possible evolutions of these communicating state machines. All possible system evolutions can be formally represented as an $L^2$TS in which the states represent the system configurations and the transitions represent the possible evolutions of a system configuration.

As a result, UCTL can be used to express properties of the dynamic behaviour of complex systems described as UML state diagrams. The ability to state structural properties of system configurations (state attributes and predicates) and not just actions (events), opens the door to the modelling and verification of structural properties of parallel systems. Examples include topological issues, state invariants and mobility issues.

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