

On the fly model checking of communicating UML State Machines¹

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Abstract. In this paper we present an "on the fly" model checker for the verification of the dynamic behavior of UML models seen as a set of communicating state machines. The logic supported by the tool is an extension of the action based branching time temporal logic μ -ACTL and has the power of full μ -calculus. Early results on the application of this model checker to a case study have been also reported.

1 Introduction

The Unified Modeling Language (UML) is a graphical modeling language for object-oriented software and systems [18,25] It has been specifically designed for visualizing, specifying, constructing and documenting several aspects of - or views on - systems. Different diagrams are used for the description of the different views.

In this paper, our aim is to define an environment for the formal verification of behavioral properties of systems modeled by a fixed number of message exchanging active objects, each of them described by a UML Statechart Diagram.

The paper proposes the use of a formal verification technique, namely model checking [5], to verify the conformance of a design with respect to desired properties. Since model checking suffers the so called "State Space Explosion" problem, that can arise when a system is composed of several parallel subsystems we have developed an on the fly algorithm for model checking UML communicating state machines. This algorithm is able to check the validity of a formula without generating the global

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model of the system bypassing the state explosion problem that makes other verification tools inapplicable.

UMC (UML on the fly Model Checker) is the results of a project recently started at IEI (now ISTI) with the purpose of doing some experimentation in three different directions. First, we are interested in testing the appropriateness of the UML methodology (and in particular UML statecharts) for the design and the specification of the dynamic behavior of a system. The question here is if we can find a subset of UML which from one side is reasonably well defined and powerful enough to allow a specification to be written without too much effort, and from the other side is still not too complex to allow a verification/analysis tools to be developed for it.

As a second theme, we are interested in investigating the kind of user interface that might help a non-expert user in taking advantage of formal specifications and verification techniques. Nowadays formal methods still encounter many obstacles in being widely used and accepted, and we believe that the kind of human interface they usually provide does play a main role in this difficulty. UML, with all its standard graphic and yet standard layout features, might present an opportunity to convey to the user a more friendly way of specifying models and their properties.

Thirdly, we have already started an interesting experience (which is still ongoing) in designing and implementing an "on the fly" model checker for full μ -calculus for networks of automata, which has resulted in the integration of the FMC tool inside the JACK environment [4]. We are now interested in exploring the advantages given by the "on the fly" approach for the verification of the dynamic behavior of UML models.

UMC, indeed, is essentially an experiment in the design of an integrated tool for the construction, the exploration, the analysis and the verification of the dynamic behavior of UML models described as a set of communicating state machines.

The present paper is organized as follows: in Section 2 we discuss the problems we have encountered in defining a formal verification environment for UML Statechart Diagrams, related in particular to the description of the formal model on which to perform the verification of behavioral properties; in Section 3 we debate the assumptions and limitations we have taken into account in the implementation of UMC by passing some of the intrinsic limits imposed by the complexity of UML; Section 4 presents the logical framework used to express behavioral properties; in Section 5 the on the fly algorithm is defined. The application of UMC to a case study is shown in Section 6. We conclude the paper with a comparison with related works together with some conclusions (Section 7).

2 UML modeling difficulties

UML is a semi-formal language, since its syntax and static semantics (the model elements, their interconnection and well-formedness) are defined formally, but its dynamic semantics are specified only informally. As already hinted in the introduction, a problem is that full UML is a very complex framework, which at a first glance

looks even too complex for what might seem to be the needs and the capabilities of a formal verification environment. Therefore have the need to identify a more tractable subset of features of UML, which still allow in a reasonable way a well-defined and consistent definition of a model.

Several approaches have been proposed in the literature for the definition of a formal semantics of UML Statechart Diagrams, e.g. [1,20,28], starting from them in UMC project we have proceeded with the process of UML subset identification in a bottom up way, adding in the time more and more features, according to the specification needs which have been identified, while more experience has been gained in the project. The difficulty of achieving a really complete support of UML features can also be observed in the current state of art of UML supporting tools. For example, we have not yet been able to find a free or inexpensive implementation allowing the design of statecharts with all their features, and even expensive environment are often lacking some of them.

A problem encountered in modeling the dynamic semantics of UML statecharts is introduced by the many aspects which UML explicitly and intentionally leaves as "implementation dependent" or "implementation defined", or simply "not specified by the standard". Examples of these "intentionally not specified" aspects are the precise semantics of queue, the precise semantics of signal transmission, the precise semantics of parallel evolutions of multiple state machine, the set of actions allowed inside a transition, and so on. For realizing a formal verification tool, the only way to deal with these aspects is either to make some own implementation choice or to handle the aspect as a parametric aspect, which could be in some way specified according to some user choice.

Another problem is that we may also find "partially defined" aspects which look like just incomplete or imprecise definition of the dynamic semantics of a state machine, without any hint on the fact that this under-specification is intentional or not. Or we may encounter contradictory / inconsistent aspects of the UML definition (e.g. the behavior in presence of composite, dynamic choice transitions), or aspects defined in a particularly ambiguous way (e.g. the handling of completion transitions).

Again a formal verification tool is forced to make its own implementation choices, but in this case the question remain on whether or not the correct choice has been made, or if a different choice left implicit behind the UML definition should have been made (an example of that being the priority of join transitions).

Another difficulty, which is intrinsically related to the UML statechart design, is that they may have a potentially infinite number of states. This happened because the given state of a state machine includes a potentially unbounded queue of events, and maybe also because the data types used and updated by the transition actions can be potentially infinite data types.

A final additional, not strictly technical, difficulty is related to the fact that it is not evident what could / should be considered as observable of a system configuration or of a system evolution from the point of view of the abstract semantics of a state machine. At least the values of the object attributes or the signals generated during the system evolution should be considered as "observable". Already this minimal assumption implies that a system evolution should contain not just one "observable

event" (as it usually happened for most process algebras) but also a certain number of them and that a system configuration should not be a "black box".

3 UMC: Assumptions and limitations

The difficulties mentioned in Section 2, and our desire to proceed in bottom up process by adding more and more features to successive running versions of the UMC prototype has led us to a certain number of assumptions and limitations built in the current version. As more experience is gained in the project assumptions might change and limitations might be removed.

3.1 UMC Assumptions

- The whole sequence of actions constituting the actions part of statechart transition, is supposed to be executed as an indivisible atomic activity, i.e. two parallel statechart transitions, fireable together in the current state-machine configuration, cannot interfere one with the other, but they are executed in a sequential way (in any order).
- Given a model constituted by more than one state machine, a system evolution is constituted by any single evolution of any single state machine. I.e. state-machine evolutions are considered atomic and indivisible.
- The propagation of signals inside a state machine and among state machines is considered instantaneous, and loss free.
- The events queue associated with a state machine handles its events in a FIFO way.
- The relative priority of a join transition is always well defined and statically fixed.

3.2 UMC Limitations

- Events: Only asynchronous signals are supported. Call events, time events, change events, events deferring are not supported.
- States: Internal transitions, Enter / Exit/ Do activities, are not supported. History states, Sync states, Choice pseudo-states are not supported.
- Transitions: Initial default transitions do not have actions, static and dynamic choice transitions are not supported. Completion transitions cannot appear in more than one region of concurrent state.
- Other: Sub-machines are not supported. Actions can only be simple assignments and sending of signals. The only data type for variables and signal parameters is constituted by 32 bits integers. Boolean and Integer expressions have some simplification.

4 μ -ACTL⁺ and UML state machines

In the previous sections we have analyzed the problems related to the definition of a formal model for UML statecharts, we now introduce the logical framework used to express the behavioral properties we wish verify on the model associated to a UML specification. The logic we consider is μ -ACTL [7], an extension with a fixed-point operator of the action based logic ACTL defined in [6], whose expressive power is the same of full modal μ -calculus [17]. μ -ACTL is a branching time temporal logic suitable to express properties of communicating systems whose behavior is characterized by the actions they perform. μ -ACTL is suitable to express properties of concurrent systems whose behavior is characterized by the actions they perform and whose semantics is defined by means of Labeled Transition Systems (LTSs). The logic can be used to define both *liveness* (something good eventually happen) and *safety* (nothing bad can happen) properties of reactive systems (with and without *fairness* constraints). A μ -ACTL formula can be built with the following syntax:

$$\Phi ::= \text{true} \mid \Phi \wedge \Phi \mid \neg \Phi \mid \text{E X}_{\{\chi\}} \Phi \mid \text{E X}_{\{\tau\}} \Phi \mid \min Z : \Phi$$

where χ are action formulae, that intuitively express sets of actions, having the following syntax:

$$\chi ::= \text{true} \mid a \mid \chi \wedge \chi \mid \sim \chi$$

and “a” is an observable action belonging to a finite alphabet of actions. τ represents instead a not visible action (not belonging to the finite alphabet of actions).

The formal semantic of μ -ACTL is given over Labeled Transition Systems. Informally, a formula is true on an LTS, if the sequence of actions of the LTS verifies what the formula states. We hence say that the formula $\text{E X}_{\{\chi\}} \Phi$ is true in a state S of an LTS when Φ is true in a successive state of S reached by an action satisfying χ and the formula $\text{E X}_{\{\tau\}} \Phi$ is true when that Φ is true in successive state of S reached by a τ action.

Starting from the basic μ -ACTL operators, some derived ones can be defined in the usual way, among them: the Hennessy-Milner [13] state modalities $[] < >$, the EF (eventually) and AG (always) formulae, and the $\max Z : \Phi$ (maximal fixed point). We refer the interested reader to [7] for a more detailed description of μ -ACTL.

In this paper μ -ACTL is extended to make possible observations on UML model evolutions and assertions on explicit local state variables of UML state machines. We will call this logic μ -ACTL⁺. Unlike most process algebras, UML state machines have an explicit set of objects attributes. This raises the question whether or not we should allow the user to specify system requirements (e.g. logic formulae), which take into account also the values of attributes during the execution. We have decided to allow this kind of internal visibility inside the system configurations and this has been achieved adding to the μ -ACTL logic a special `ASSERT` state predicate.

Now χ formulae become evolution predicates, and “a,, the observation of a signal event being sent to a target object (here square parenthesis are used to denote optional parts):

$$\chi ::= \text{true} \mid [\text{target.}] \text{event}[(\text{args})] \mid \chi \wedge \chi \mid \sim \chi \mid \chi \vee \chi$$

starting from this the syntax of $\mu\text{-ACTL}^+$ is the following:

$$\Phi ::= \text{true} \mid \Phi \wedge \Phi \mid \neg \Phi \mid \text{EX}_{\{\chi\}} \Phi \mid \text{EX}_{\{\tau\}} \Phi \mid \max z : \Phi \mid \text{ASSERT}(\text{VAR}=\text{value})$$

$\text{ASSERT}(\text{VAR}=\text{value})$ is true if and only if in the current configuration the attribute VAR has value equal to "value".

Following the above syntax we will write using $\mu\text{-ACTL}^+$ formulae such as:

$$\text{EX}_{\{\text{Chart.my_event}\}} \text{true}$$

that means: in the current configuration the system can perform an evolution in which a state machine sends the signal `my_event` to the state machine `Chart`.

Or the formula:

$$\text{EX}_{\{\text{my_event}(3)\}} \text{true}$$

that means: in the current configuration the system can perform an evolution in which a state machine sends the signal `my_event(3)` to some other state machine.

The action expression τ is supposed to match instead any system evolution, which does not send any signal.

The following formula:

$$\text{AG}((\text{EX}_{\{\text{my_event}\}} \text{true}) \rightarrow \text{ASSERT}(\text{Object.Attribute}=\text{Value}))$$

meaning that the signal `my_event` can be sent, only when the specified attribute of the specified object has the specified value.

5 The on the fly model-checking approach

Our approach to the "on the fly" model checking of a $\mu\text{-ACTL}^+$ logic formula has been initially presented in [12]. In that case the system to be verified was defined by a network of synchronized agents working in parallel. The model checker, named FMC, was included in Jack [4], an environment based on the use of process algebras, automata and temporal logic formalisms, supporting many phases of the system development process. The model checker presented here, UMC, is based on the same ideas of FMC, but working over a set of communicating (i.e. exchanging signals) UML State machines.

Even though the code for both tools FMC and UMC has been almost completely rewritten several times, the underlying logic schema has remained the same.

The basic idea behind FMC and UMC is that, given a system state, the validity of a formula on that state can be evaluated analyzing the transitions allowed in that state, and analyzing the validity of some sub-formula in only some of the next reachable states, in a recursive way, as shown by the following simplified schema (E: Env

represents the “current context” in which a given subformula is evaluated, which gives a precise meaning (in terms of already started computations) to the free variables which appear in it):

```

Evaluate (F: Formula, E: Env, S: State) is
  if we have already done this computation and
    the result is available then
    return the already known result
  elsif we are already trying to compute F in S with E then
    return true or false depending on maximum or minimum
      fixed point semantics
  else
    Keep track of the fact that we are trying to compute
      F in S with E (e.g. push the pair (F,E,S) in a stack)
    for each sub-formula F' and
      next state S' which needs to be computed loop
      call recursively Evaluate (F', E', S');
      if the result of Evaluate (F', E', S') is sufficient
        to establish the result of evaluate (F,E,S)
    then
      exit from the loop;
    end if
  end loop
  (at this point we have in any case a final result)
  Keep track of the fact that we are
    no longer trying to compute F in S with E;
  (e.g. pop the pair (F,E,S) from the stack)
  Possibly keep track of the performed computation and result
  (e.g. push the triple (F, E, S, result) in a hash
table)
  return the final result
end if
end Evaluate;

```

The big advantage of the on-the-fly approach to model checking is that hopefully only a fragment of the overall state space might need to be generated and analysed to be able to produce the correct result (cf. [2,9]). This approach seems particularly promising when applied to UML state machines (or groups of communicating state machines) because it can easily be extended also to the case of potentially infinite state space, as it may happen for UML state machines. Indeed, a problem of the above evaluation schema is that, in case of infinite state machines, it might fail to produce a result even for some cases in which a result might be produced in a finite number of steps. This is a consequence of the "depth first" recursive structure of algorithm. The solution taken to solve this problem consists in adopting a bounded model checking approach [3], i.e. the evaluation is started assuming a certain value as maximum depth limit of the evaluation. In this case if a result of the evaluation a formula is given inside the requested depth, then the result holds for the whole system, otherwise the depth limit is increased and the evaluation restarted.

This approach, initially introduced in UMC to overcome the problem of infinite state machines, happens to be quite useful also for another reason. Setting a small initial depth limit, and a small automatic increment of it at each re-evaluation failure, when we finally find a result we can have a reasonable (almost minimal) explanation for it, and this could be very useful also in the case of finite states machines.

6 UMC and the Airport Case Study

Let us consider, as a toy example, a system constituted by two airports, two passengers (one at each airport), and a plane. The plane is supposed to carry at exactly one passenger and flies (if it has passengers) between the two airports. Before boarding the plane the passenger must perform the check in. After the plane has arrived at the destination airport, the passenger deplanes. We contemplate only one observable action performed by the passenger during the flight, namely the consumption of a meal. Let us consider a scenario where a Passenger boards a plane in Airport1, flies to Airport2 and deplanes there.

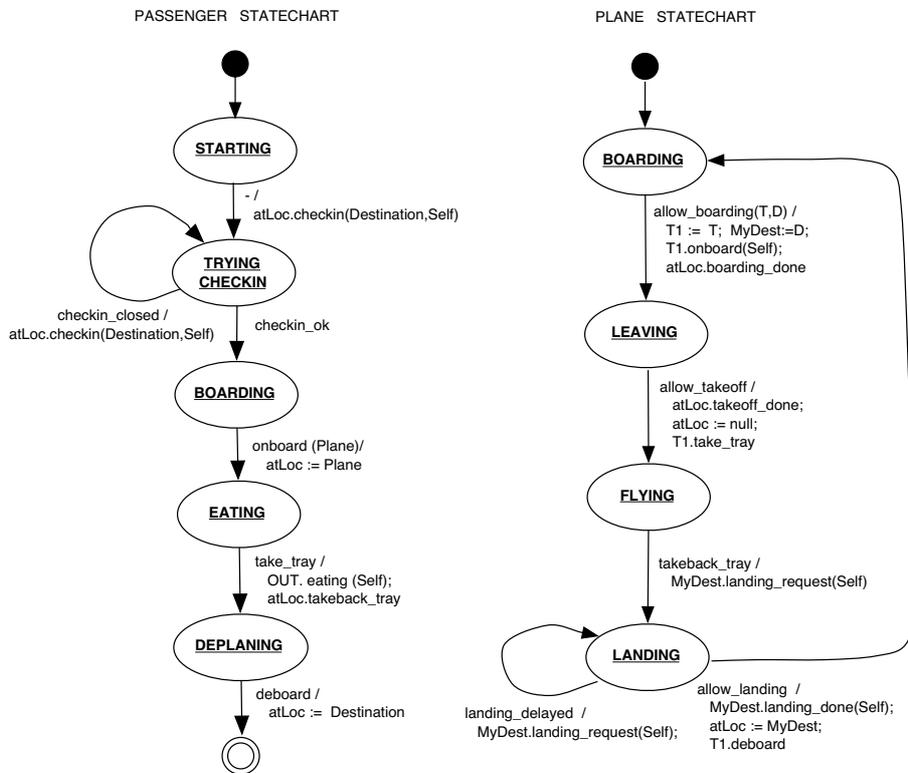


Figure 1: Plane and Passenger Statecharts

6.1 Model Definition

The model under investigation is specified by a textual description of a set of UML statechart diagrams, one for each class of objects which constitute the system, and by a set of object instantiations. This description of the classes of the model can be di-

rectly edited in a simple textual form, or extracted from an UML model description given in the XMI format. In Figure 1, and 2 we show the statechart diagrams of classes Plane, Passenger and Airport. In Figure 3 we show the UMC textual notation used to represent the Passenger statechart.

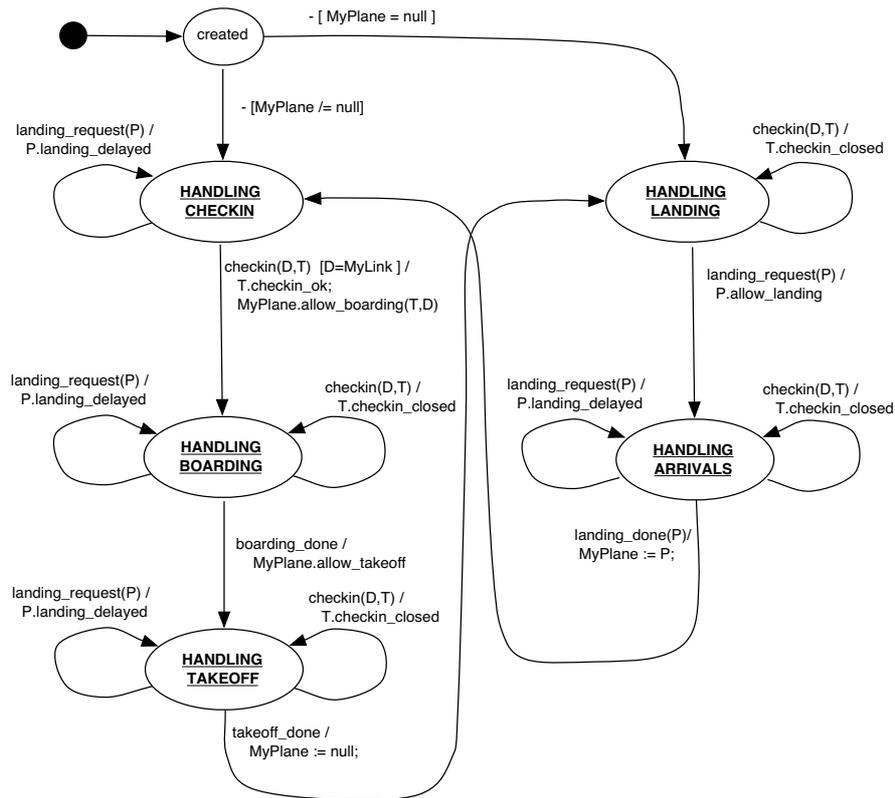


Figure 2: Airport Statechart

The initial deployment of the system is defined by the following object declarations:

OBJECT	CLASS	INITIAL VALUE FOR ATTRIBUTES
Airport1:	Airport	(MyLink => Airport2, MyPlane => Plane1);
Airport2:	Airport	(MyLink => Airport1)
Traveler1:	Passenger	(AtLoc => Airport1, Destination => Airport2)
Traveler2:	Passenger	(AtLoc => Airport2, Destination => Airport1)

```
Plane1: Plane (AtLoc => Airport1)
```

```
Class Passenger
Vars: atLoc:obj, Destination:obj
Events: checkin_ok, checkin_closed, onboard(P:obj),
          take_tray, deboard
State Top = STARTING, TRYING_CHECKIN, BOARDING,
          FLYING, DEPLANING, FINAL

STARTING -( -/atLoc.checkin(Destination,Self) )-> TRYING_CHECKIN
TRYING_CHECKIN -( checkin_closed /
                 atLoc.checkin(Destination,Self) )-> TRYING_CHECKIN
TRYING_CHECKIN -( checkin_ok ) -> BOARDING
BOARDING -( onboard(P) / atLoc := P )-> FLYING
FLYING -( take_tray /
          OUT.eating(Self); atLoc.takeback_tray )-> DEPLANING
DEPLANING -( deboard / atLoc := Destination )-> FINAL
```

Figure 3: textual notation for passenger statechart

6.2 Model exploration

Once a description of a system has been successfully loaded its initial configuration can be graphically visualized as a set of statecharts, in which the currently active substates are highlighted. The allowed evolutions from the current configurations are shown and they can be manually selected to visualize the subsequent configurations reachable by applying them. The LTS representing all the possible system evolution steps can be graphically visualized as a click sensitive graph. Clicking over a node leads to the visualization of the structure of the node (its active, states, the values or its variables, the content of the events queue).

The whole formal model for our airport scenario is an LTS containing 240 states and 595 transitions.

6.3 Model verification

After a system has been loaded, it is possible to enter a μ -ACTL⁺ formula to be evaluated over its model. Once a formula has been edited its on the fly evaluation starts.

In our case study we could be interested, for example, to check if it is true that a passenger can eat (signal `eating(Traveler1)`), only when the plane is flying (`Plane1.atLoc=null`). This can be done by checking the truth of following μ -ACTL⁺ formula:

```
AG((EX{eating(traveler1)}true) ->
    (ASSERT(Plane1.atLoc=Plane1=1) & ASSERT(Plane1.atLoc=null))
```

The evaluation of this formula asks that the whole reachable state space has to be traversed, not benefiting in this way of the on the fly approach.

This instead happens for the following formula, that means there exists an infinite (unfair) path along which nobody eats:

```
max Z: EX {~ eating} Z
```

This formula is TRUE on our model and only a small fragment of the state space is visited to prove it.

Let us consider now the formula expressing the property: it is always true that, if flying, Plane1 will eventually land.

```
AG (ASSERT(Plane1.atLoc=null)-> AF ~ASSERT (Plane1.atLoc=null))
```

This formula is false on our system and at a first glance it may appear surprising.

Once the plane is moving from Airport1 to Airport2, it might happen that the objects Airport2 and Traveler2, both, monopolize the system evolutions cycling in their attempt to try to check-in and refusing it. Under these circumstances the unfairness of the system scheduler might prevent the Plane1 to signal its landing request. Fairness issues are likely to play a relevant role in UML as constraints for UML verifications, and the power of full μ -ACTL⁺ is needed to express these properties in a general way.

After a formula has been evaluated, a complete explanation, in the style of the counterexample facilities of classical model checking tools, can be visualized (both a graphic and in textual format) showing the logic steps which have led to the result. Each step of the explanation is essentially an assertion of the kind:

The formula <F1> **is true / false in configuration** <C1>
because <F2> **is true /false** <C2>
and because <F3> **is true /false in configuration** <C3>
and because

From each step of this explanation we can directly visualize the set of system evolution starting from the configuration to which the step refers.

7 Related Works and Conclusions

Linear-time model checking of UML Statechart Diagrams is addressed in [19], [10] and [24]. In [11] a simple (branching time) model-checking approach to the formal verification of UML Statechart Diagrams was presented exploiting the “classical” model checking facilities provided by the AMC model checker available in JACK. We are currently aware of three available tools for model checking UML systems described as sets of communicating state machines. HUGO [22,26] and ν UML [21] take the approach of translating the model into the Promela language using SPIN [14] as the underlying verification engine. We have not had direct experience with these tools, but clearly in this case the properties to be verified need to be mapped into LTL logic. While ν UML is restricted to deadlock checking, HUGO is mainly intended to verify whether certain specified collaborations are indeed feasible for a set of UML state machines. In both cases, the UML coverage of the tools is wider than ours because it includes UML call operations, history states, and internal state activities. A timed version of HUGO (called HUGO/RT [16]) has also been developed, which maps into the UPPAAL verification engine, instead than into SPIN.

A third interesting approach is that one adopted in the ongoing UMLAUT [15,27] project. In this case an UML execution engine has been developed, adopting the Open Caesar standard interface of the CADP environment. In this way all the CADP [8] verifications tools (including the “on the fly” Evaluator tool [23]) can be applied also to this new engine.

As far as we now, FMC and UMC are the only “on the fly” tools supporting full μ -calculus (SPIN uses LTL, CADP Evaluator the alternation free μ -calculus).

The fact of being able to state and check also structural properties of system configurations (state attributes and predicates) and not just events, opens the door to the modelling and verification of several structural properties of parallel systems, like topologic issues, state invariants, and mobility issues.

The approach adopted in UMC seems promising but there is still a lot work to do. Certainly the UMC coverage must be extended to include at least call operations, events deferring, and state internal activity. Moreover the semantic / logic issues still need to be assessed (i.e. precisely which kind of property do we want to verify, and which kind of optimizations do they allow to be implicitly performed by the tool). The current alpha-version of the UMC prototype (which is now at version 2.5) is accessible “online” through its www interface at the address <http://matrix.iei.pi.cnr.it/umc/demo>.

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